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Biclustering Learning of Trading Rules

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Abstract—Technical analysis with numerous indicators and patterns has been regarded as important evidence for making trading decisions in financial markets. However, it is extremely difficult for investors to find useful trading rules based on numerous technical indicators. This paper innovatively proposes the use of biclustering mining to discover effective technical trading patterns that contain a combination of indicators from historical financial data series. This is the first attempt to use biclustering algorithm on trading data. The mined patterns are regarded as trading rules and can be classified as three trading actions (i.e. the buy, the sell, and no-action signals) with respect to the maximum support. A modified K-NN method is applied to classification of trading days in the testing period. The proposed method (called BIC-KNN) was implemented on four historical datasets and the average performance was compared with the conventional buy-and-hold strategy and three previously reported intelligent trading systems. Experimental results demonstrate that the proposed trading system outperforms its counterparts and will be useful for investment in various financial markets.

Index Terms—Machine learning, Biclustering, Technical analysis, Trading rules.

I. INTRODUCTION

TRADING on the stock market has been a popular investment channel due to its potential for excess profits. It is a non-linear dynamic system that is influenced by a lot of factors such as national policies, the economic environment, supply-demand relationships, et al. However, it is not easy for investors to make a correct trading decision at the right time, because the stock market is a highly complicated and dynamic system [1] [2]. Therefore, it is of great benefit to analyze the price movement and provide trading rules to guide investors in making trading decisions.

Technical analysis aims at devising appropriate trading rules in the stock market. It studies the historical data, primarily price and volume, to forecast the direction of prices and make trading decisions based on the predictions [3]. Voluminous literature exists on technical analysis in various financial domains. Results obtained in the 1960s and 1970s supported the efficient market hypothesis [4] [5], one of the most widely accepted theories in economics, which states that the financial markets are efficient and the current market price fully reflects

all the available information. There is no opportunity to consistently gain profit over the average in the market, and it is pointless to predict future market price behavior, whether by fundamental analysis or technical analysis. However, a number of studies since the 1980s have implied that historical data can help to predict future prices [6] [7] [8] [9] [10].

In recent years, much research into the stock market using data mining and computational intelligence techniques have shown positive results. Frequently used techniques include genetic programming (GP), artificial neural networks (NN) and template matching. Liu [11] presents a decision-making model de-scribed by a recurrent neural network for dynamic portfolio op-timization. The results substantiated the effectiveness and illus-trated the characteristics of the proposed neural network. Potvin et al. [12] used genetic programming to generate short-term trading rules on stock markets. Instead of using a composite stock index, trading rules were adjusted to individual stocks from the Toronto stock exchange market. Lin et al. [13] enhanced conventional technical analysis with genetic algorithms (GA) by learning trading rules from history for individual stock, and then combined different rules together with Echo State Network to provide trading suggestions. Chen et al. [14] used Genetic Network Programming with Sarsa Learning to create a stock trading model. Kwon et al. [15] proposed a hybrid system combining the recurrent neural network (NN) and a genetic algorithm for stock trading. Chavarnakul et al. [16] explored the profitability of stock trading by using a neural network model developed to assist the trading decisions of the volume adjusted moving average (VAMA) and the ease of movement (EMV). Chien et al. [17] proposed a GA-based algorithm used to build an associative classifier that discovers trading rules from numerical technical indicators. Wang et al. [18] examined the potential profit of bull flag technical trading rules using a template matching technique based on pattern recognition for the Nasdaq Composite Index (NASDAQ) and Taiwan Weighted Index (TWI). The results indicated that the trading rules correctly predicted the direction of change in the NASDAQ and TWI. Leigh et al. [8] implemented a recognizer for two variations of the bull flagtechnical charting heuristic and used the recognizer to discover trading rules on the NYSE Composite Index. Out-of-sample results indicated that the rules were effective.

Basically, all these methods belong to technical analysis and all the research showed that trading success can be achieved with these methods. However, drawbacks exist for all these methods. The GP is designed for global optima, which cannot guarantee to find the best solution, and it is difficult to avoid the problem by making appropriate design choices. The NN are non-linear and non-parametric models. Although the NN is dominant in stock prediction, the models have limitations due to noise and complex dimensionality of

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data, resulting in unconvincing results. Therefore, to deal with the high dimension of the input data matrix, feature selection and feature learning are mainly two ways for dimensionality reduction[19], and matrix factorization approaches such as singular value decomposition(SVD) and nonnegative matrix factorization(NMF) has recently been used for representation of the original data matrix [20]. In addition, the problem of overfitting in the NN cannot always be easily avoided. Template matching is used for the fitting, but the fitting process may be unstable, which may cause the rising flag template fit to be lower than that of the declining flag and lead to missing the trading opportunities.

It has been empirically and theoretically demonstrated that learning technical indicators jointly always gains better performance than learning each indicator independently[16] [21]. To this end, we propose a novel method incorporating a biclustering algorithm and the K nearest neighbor (BIC-KNN) to discover significant technical trading patterns and to determine the trading actions. This is the first attempt to use biclustering algorithm on financial data series. The biclustering algorithm is a type of data mining method that can extract coherent patterns, each of which contains a subset of indicators with different time lengths. Thus, a combination of different technical indicators in a coherent pattern can be found using the biclustering method if they behave in a similar manner for the same sort of turning points. The detected patterns are regarded as trading signals including the buy, sell and no-action signals, and are eventually used in deciding trading actions in financial markets. Furthermore, the proposed method is a framework that can be extended to add more technical indicators, different time spans and trading terms, which makes it a general model that very flexible for investors in various financial markets.

The remainder of this paper is organized as follows. Section II provides a brief introduction of biclustering algorithms. Section III describes the proposed algorithm. Section IV shows the experimental results. Section V provides discussions on the proposed method and concludes this study.

II. BICLUSTERING ALGORITHMS

Clustering, as a fundamental task of many machine learning, data mining and pattern recognition problems[22], identifies objects with the same attributes or the same functions. Given a data matrix, a traditional clustering algorithm classifies the data along either the row or the column separately. However, it is difficult to extract local coherent patterns that include subsets of rows and subsets of columns. Often, clustering objects under a subset of attributes would be more beneficial for mining important information. For instance, a trader may heavily rely on a small number of technical indicators that provide the most useful predictions to the market to make trading decisions. As a result, how to find these useful indicators (i.e. a subset from all indicators considered) that have similar behaviors in predicting turning points (a subset of trading days) is an interesting problem in practice. To solve this problem, we need to partition the data in both the row and column directions. This approach has been termed

as biclustering. Biclustering is actually a special branch of clustering algorithms because it clusters the data along the row and the column simultaneously in a two-dimensional data matrix [23].

The term biclustering was first used by Cheng and Church [24] in gene expression data analysis. Names such as coclustering, bidimensional clustering and subspace clustering are often used in the literature to refer to the same problem formulation [25]. In [24], an approach known as mean squared residue score (MSRS) was introduced to assess the coherence of the elements of a bicluster. A bicluster is a sub-matrix with a coherent pattern in a data matrix. Given a $N_r \times N_c$ data matrix, a bicluster can be defined as a subset of rows and a subset of columns of X . It can be expressed as a pair (R, C) , where $R \subseteq \{1, \dots, N_r\}$ is a subset of rows and $C \subseteq \{1, \dots, N_c\}$ is a subset of columns in the dataset. The goal of biclustering is to identify a subset of rows with certain coherence properties under a subset of the columns. The MSRS is formulated as follows:

$$\begin{aligned} H(R, C) &= \frac{1}{|R||C|} \sum_{i \in R, j \in C} (a_{ij} - a_{iC} - a_{Rj} + a_{RC})^2, \\ a_{iC} &= \frac{1}{|C|} \sum_{j \in C} a_{ij}, \\ a_{Rj} &= \frac{1}{|R|} \sum_{i \in R} a_{ij}, \\ a_{RC} &= \frac{1}{|R||C|} \sum_{i \in R, j \in C} a_{ij} \end{aligned} \quad (1)$$

where a_{ij} denotes the element value at the i th row and j th column in the bicluster, $H(R, C)$ the value of MSRS for the bicluster, and δ is a homogeneity threshold defining the maximum allowable dissimilarity within the elements of the bicluster. A submatrix is called a δ bicluster if $H(R, C) \leq \delta$ for some $\delta \geq 0$. The homogeneity threshold is set by users.

According to a survey provided by Madeira and Oliveira [25], biclusters can be grouped into four types: biclusters with constant values, constant values in rows or columns, coherent values, and coherent evolutions. Fig. 1 illustrates ten typical examples for these four types of biclusters. The first three are represented by the numeric values in the data matrix, as shown in Figs. 1a, 1b, 1c, 1d, and 1e, which represent biclusters with constant values, constant values in rows, constant values in columns, additive coherent values and multiplicative coherent values, respectively. Figs. 1f, 1g, 1h, 1i, and 1j represent biclusters with overall coherent evolution, coherent evolution in rows, coherent evolution in columns, coherent evolution values in columns, and coherent sign changes in rows and columns, respectively. A large number of successful applications exist for biclustering in many domains, such as biological data analysis, target marketing, feature selection, and other data mining applications [26] [27] [28] [29].

III. METHODS

Technical analysis tends to forecast future price movement using certain rules based on the study of statistical data

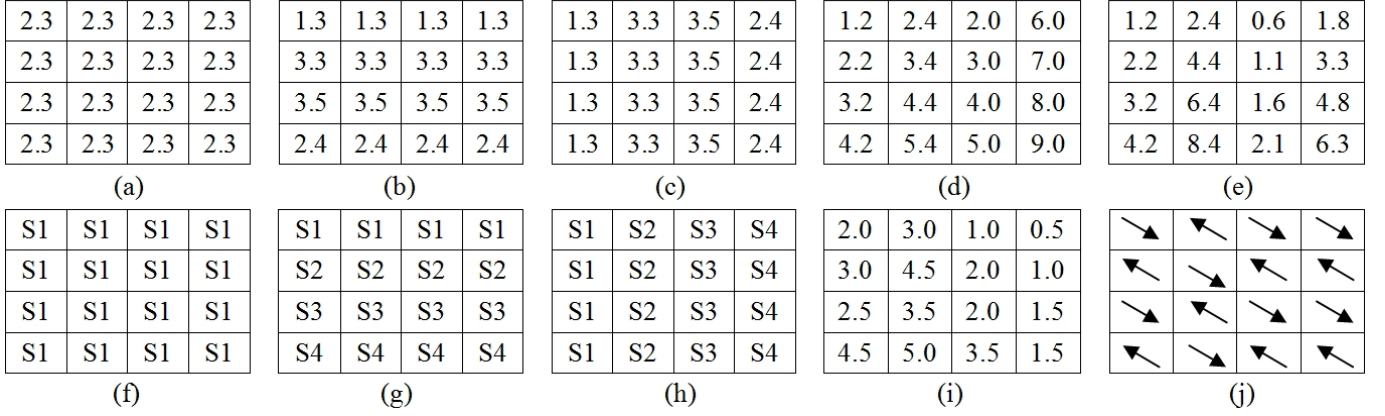


Fig. 1: Examples of different types of biclusters. (a) constant values, (b) constant values in rows, (c) constant values in columns, (d) additive coherent values, (e) multiplicative coherent values, (f) overall coherent evolution, (g) coherent evolution in rows, (h) coherent evolution in columns, (i) coherent evolution values in columns and (j) coherent sign changes in rows and columns.

that has been generated through market transactions. These trading rules are based on charts or technical indicators that are mathematical formulas that use historical data as input and then return an output signal, which can help investors to make decisions in the markets. As mentioned in section II, a bicluster defined by a subset of rows (objects) and a subset of columns (attributes) indicates a submatrix, which can be treated as a local coherent pattern (i.e. a subset from all indicators considered that have similar behaviors under a subset of trading days). The detected coherent patterns, including a number of typical turning modes, are identified as trading rules. Therefore, we make use of the biclusters found in a data matrix to generate trading rules in this section.

For a stock or a financial composite index, historical data series are used to form a data matrix, in which the rows correspond to the trading days and the columns correspond to the technical indicators and future return. Observing that local information and manifold information are both crucial for data clustering, and we are inspired from the method proposed by Huang[28] and Yang et al.[30] [31] in our work for mining trading rules, we propose an effective biclustering algorithm that converts the problem of searching for biclusters in the data matrix into two procedures: (1) an agglomerative hierarchical clustering algorithm of rows for each column in the data matrix, and (2) a search for the biclusters associated with the clustered rows found in the first procedure. A large number of biclusters may exist after the two procedures, and from these, two factors (i.e., the future returns and the evaluation function) are thereafter taken into consideration. The detected biclusters are then transformed into trading signals with the KNN method. Though the idea of using biclustering algorithm to cluster data objects on a selected subset of features seems to be simple, it detects local coherent patterns from the data matrix well. There are numerous models such as intra-day, daily, weekly, and monthly trading for automatic stock trading, depending on behavioral scope. This study considers only the daily trading model.

A. Data preparation

For a stock or a financial composite index, a data matrix is constructed using historical data where the rows correspond to trading days and the columns correspond to 26 technical indicators with different periodic parameters and future returns. Seven popular technical indicators are chosen for this study to form the data matrix. They are the rate of change (ROC), the exponential moving average (EMA), the average directional index (ADX), the average true range (ATR), simple moving average (SMA), the Williams percentage range (%R) and relative strength index (RSI). With different time lengths associated with each indicator, there are a total of 26 features adopted as the first section of the columns. Table I shows the technical indicators with the different periodic parameters adopted in this study. Furthermore, future returns are placed in the data matrix as the second section of the columns. They can be obtained by averaging the returns of the following trading days over a period of time. The number of following trading days is determined by users according to their respective applications.

TABLE I: CALCULATION PERIODS OF THE TECHNICAL INDICATORS.

Indicators	Period1	Period2	Period3	Period4	Period5	Period6
ROC	12	24	36	\	\	\
EMA	12	24	36	\	\	\
ADX	14	28	42	\	\	\
ATR	14	28	42	\	\	\
SMA	10	20	30	40	\	\
%R	9	18	27	36	\	\
RSI	6	12	18	24	30	36

Fig. 2 illustrates the structure of the data matrix. The elements in the data matrix are assigned the values of the indicators (columns 1 to 26) and the future returns (column 27) corresponding to the trading days. All the technical indicators of a stock or a composite index are computed using the historical data, including the closing prices and transaction volumes. Therefore, a data matrix with a width (column) of 27 and a height (row) of the same as the number of trading

Each column corresponds to a single technical indicator

30/06/2010							
29/06/2010							
⋮	⋮	⋮	⋮	⋮		⋮	⋮	⋮
02/07/1992							
01/07/1992							
30/06/1992							
	ROC (Δ12)	ROC (Δ24)	ROC (Δ36)	EMA (Δ12)		RSI (Δ30)	RSI (Δ36)	Returns (column 27)

DATA MATRIX

Fig. 2: Data arrangement for the matrix. In the data matrix, each row corresponds to a trading day and each column corresponds to a technical indicator with a specified time length. Column 27 is the sequence of future returns, each of which corresponds to a trading day.

days in the training period can be constructed. Please note that the formation of the data matrix in this study can be regarded as an example and readers can use other technical indicators to form different data matrices for their applications.

It is commonly considered that the price movement can be described by the percentage changes of the price in the sequence of trading days. We replace the original value of elements with the percentage of difference between the original values and the closing prices of corresponding trading days on the columns of the SMA and EMA. The procedure is described by

$$PD_MA(i, j) = \frac{MA(i, j) - CP(i)}{CP(i)} \times 100\% \quad (2)$$

where the $CP(i)$ denotes the closing price at the i th trading day, $MA(i, j)$ denotes the SMA or the EMA with a periodic parameter j at the i th trading day, and $PD_MA(i, j)$ denotes the percentage of difference between $MA(i, j)$ and $CP(i)$.

Since the financial market is time variable and its price variation is a very dynamic system, this environment motivates a need for reassessment of the price movements. Therefore, in column 27, before computing the future return, the closing price corresponding to each trading day is firstly replaced by the mean closing price of the following n trading days (denoted by CP_ave_i) to reflect the price movement trends more convincingly as below,

$$CP_ave_i = \frac{1}{n} \sum_{m=i}^{i+n-1} CP_m \quad (3)$$

where CP_i is the closing price at the i th trading day. In this study, we consider short-term investment and set the parameter n to be 10. Then the future return in column 27 corresponding to each trading day is computed as

$$FRV_i = \frac{CP_ave_i - CP_i}{CP_i} \times 100\% \quad (4)$$

where FRV_i denotes the future return in percentage corresponding to the i th trading day, which represents the moving direction of price in a short period.

In order to identify the trends more explicitly in column 27, we use 1 to denote an upward trend, -1 for a downward trend, and 0 movement for a sideways trend in the n following days. If the value of $FRV_{(i,n)}$ is larger than a threshold T_t , it is set to 1; if smaller than $-T_t$, it is set to -1 . Otherwise, it is set to 0. In this paper, T_t is 0.5%.

Because the values of different technical indicators vary greatly, we apply a normalization procedure to each column of the technical indicators to map the data into a range of $[0, 1]$. This procedure is described by

$$V_n(i, j) = \frac{V_o(i, j) - V_{\min}(j)}{V_{\max}(j) - V_{\min}(j)} \quad (5)$$

where the $V_o(i, j)$ denotes the original value of the j th technical indicator at the i th trading day in the data matrix, the $V_{\min}(j)$ denotes lower bound of the j th technical indicator, the $V_{\max}(j)$ denotes the upper bound of the j th technical indicator, and the $V_n(i, j)$ denotes the normalized value of the j th technical indicator at the i th trading day.

B. Discovery of Biclusters

Having formed the data matrix, we search for the biclusters that are a result of the trading rules. Each bicluster has constant columns under a subset of indicators, as shown in Fig. 1c. On this occasion, different trading rules can be represented by a different subset of technical indicators. This means that the combination of these indicators occur multiple times during the trading days in the training set. The pattern indicated by these indicators has a high possibility to occur again, and may be a useful trading signal. Consequently, using an algorithm to find biclusters from historical financial data is necessary. Meanwhile, it is obviously noted that each indicator should take the same, or similar values for different rows in a discovered trading pattern. Therefore, we propose an algorithm to find the biclusters with constant columns (Fig. 1c) from the data matrix.

The first step is to find similar elements in a single column. An agglomerative hierarchical clustering (HC) algorithm is initially performed on each column of the data matrix. The average linkage is used and a distance threshold T_{hc} is pre-determined to measure the similarity of elements to each of the columns of the data matrix. The detected clusters from all columns are treated as bicluster seeds and placed in an HC_Set . Any of the bicluster seeds can be expressed as a pair (R, C_j) , where $R \subseteq \{1, \dots, N_r\}$ is a subset of rows and C_j is one of the columns.

The next step is to expand each bicluster seed along the column direction. For a bicluster seed (denoted by BS) from HC_Set , we process each column in N_c , other than C_j , one by one. A new column can be added to BS if the newly formed sub-matrix satisfies the criterion of $MSRS$ (i.e. the $MSRS$ score is less than a preset threshold T_{sd}). This procedure is repeated until no new column can be added to BS , and then the new bicluster seed with expansion in columns can

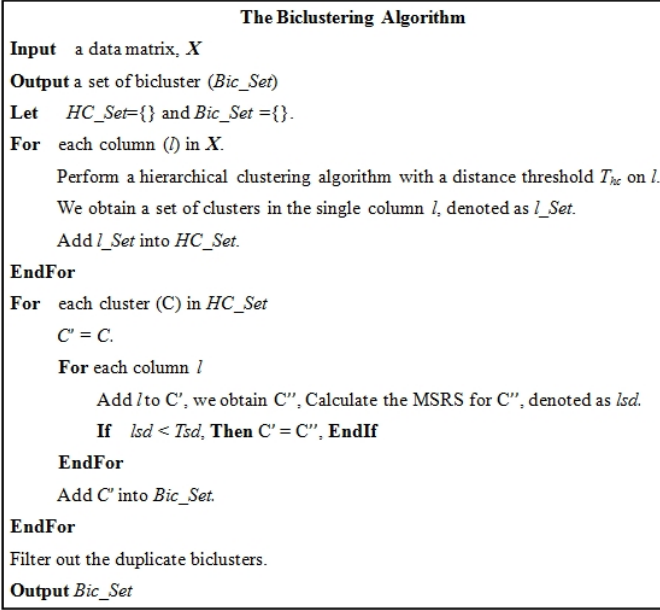


Fig. 3: The biclustering algorithm.

be regarded as a bicluster that is placed in Bic_Set . It is worth noting that the bicluster may contain only one column after the expansion, and this is also deemed as a real bicluster. After this procedure is performed for all bicluster seeds, the Bic_Set contains the final output of biclusters, any of which is expressed as (R, C) , $R \subseteq \{1, \dots, N_r\}$ and $C \subseteq \{1, \dots, N_c\}$. The flow chart of the expanding procedure is shown in Fig. 4.

Note that the search of the biclusters is applied to the sub-matrix, including columns 1-26, without considering the column of future return. The type of a bicluster is then determined by the future returns in column 27. A valid bicluster should contain at least five rows in order to be used as a robust trading rule. Furthermore, when two seed biclusters exist, constructed by the same subset of rows but different columns, (R, C_x) and (R, C_y) , the expanding procedure may produce the same bicluster. In this case, duplicate biclusters should be filtered out, keeping only one. The biclustering algorithm is described in Fig. 3.

C. Classification of the biclusters

A bicluster is translated into a trading rule by averaging each column. Because each column of a bicluster corresponds to a specific technical indicator, the output trading rule is a vector where the value of an element is the mean of the corresponding indicators values over the trading days included by the bicluster. An effective trading rule can help the trader to make a trading decision by predicting a monotone moving direction of the financial price.

Three types of trading actions occur in the stock market, i.e. buy, sell and no action, so all of the trading rules are then classified into three trading sets: buy signal set (S_b), sell signal set (S_s) and no-action set (S_n). This study defines a support-based metric as a measure to help make the classification, which is expressed as

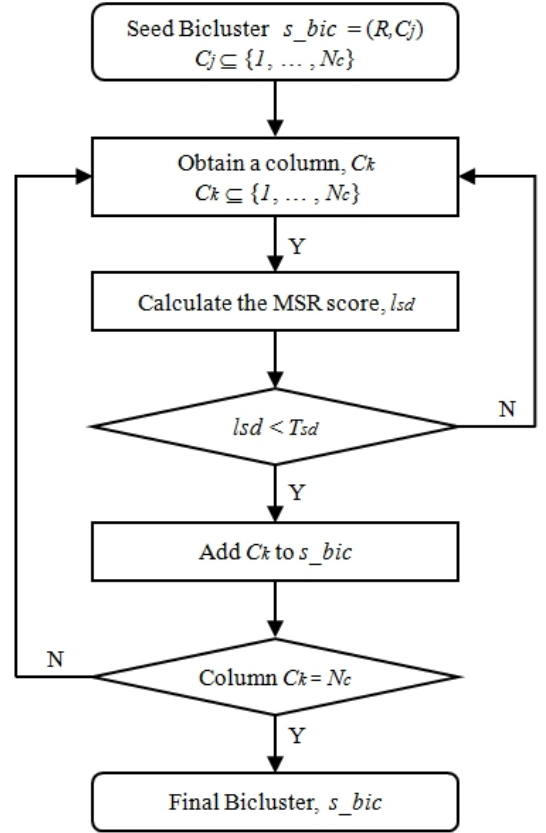


Fig. 4: The flow chart of expanding a bicluster seed.

$$\begin{aligned}
 supp(S_b) &= \frac{No.ofrowswithFRV \geq T_t}{Allrows}, \\
 supp(S_s) &= \frac{No.ofrowswithFRV \leq T_t}{Allrows}, \\
 supp(S_n) &= \frac{No.ofremainingrows}{Allrows}
 \end{aligned} \tag{6}$$

where FRV denotes the future return according to Eq.(4), $supp(S_b)$, $supp(S_s)$, $supp(S_n)$ denote the supports of the buy signal, the sell signal and the no-action, respectively.

For a bicluster, three support values ($supp(S_b)$, $supp(S_s)$, $supp(S_n)$) can be calculated according to Eq.(6). To make a trading decision, we have to know the maximum of the supports, as follows.

$$T(\bullet) = \max(supp(S_b), supp(S_s), supp(S_n)) \tag{7}$$

where T denotes the maximum value among $supp(S_b)$, $supp(S_s)$ and $supp(S_n)$, indicating that the type of the bicluster is determined by the signal with the largest support.

To obtain more reliable trading signals, we select the biclusters whose T is larger than a pre-defined threshold T_{pre} as a valid trading rule. Although larger T_{pre} results in more reliable trading signals, T_{pre} is empirically set to 0.7 in this paper to avoid inadequate valid trading rules found. For instance, given that $supp(S_b) = 0.82$, $supp(S_s) = 0.13$, and $supp(S_n) = 0.05$, respectively, the bicluster is classified as a buy signal and put into the buy signal set S_b , because $T = \max(supp(S_b),$

$\text{supp}(S_s), \text{supp}(S_n)) = \text{supp}(S_b) = 0.82$ is greater than T_{pre} . Therefore, this bicluster is transformed into a trading rule regarded as a buy signal.

D. Determination of trading actions using K-NN method

Two trading strategies[32] (called strategy 1 and strategy 2) are employed in this study – described below in Table II. Transaction fee is not considered in this study.

TABLE II: TWO TRADING STRATEGIES ADOPTED IN THIS STUDY

Strategy	Descriptions
1	If there is no position, open a long position when the indicators of current trading day conforms to a buy signal. Thereafter, close it when the indicators of a subsequent trading day conforms to a sell signal. Repeat this trading way during the testing period.
2	If there is no position, open a position when the indicators of the current trading day conforms to either a buy or a sell signal. If a position exists, close it when meeting a reversal trading signal and open a reversal position at the same trading day. Repeat this trading way during the testing period.

In the testing period, the trading actions are determined based on the matching of trading rules and trading days. For each trading day, the values of all the technical indicators are calculated. Since a trading rule is a vector of technical indicators with specific values, a trading day is considered to match a trading rule when the values of the corresponding technical indicators of the trading day are very similar to the values of the corresponding technical indicators of a trading rule. In this study, the root-mean-square (RMS) of the corresponding technical indicators is used to measure the similarity between trading day and trading rule.

$$RMS = \frac{\sqrt{\sum_{k \in ST} (V_{td}(k) - V_{tr}(k))^2}}{n_k} \quad (8)$$

where ST denotes the set of technical indicators of a special trading rule, n_k denotes the number of indicators in ST , $V_{td}(k)$ denotes the value of the indicator (corresponding to the k th indicator in ST) for the current trading day, and $V_{tr}(k)$ denotes the value of k th indicator in the trading rule.

Given a pre-defined threshold T_{rms} , a neighboring region is defined for each trading day in the testing period. Several trading rules may fall into the region (i.e. $RMS \leq T_{rms}$). In this study, T_{rms} is set to the mean of all calculated RMS between every trading day and every trading rule in the training period, thus there would be different values of T_{rms} for different training sets. We then use the K nearest neighborhood (K-NN) method as a classifier [33] to determine the trading signal for the current trading day. We set K to 5 in this study. In the first case, there is no trading rule falling into the neighborhood, so the trading day provides no trading signal, suggesting no-action on the next trading day. In the second case, there are trading rules falling into the neighborhood of a trading day. We take into account the five nearest rules. Based on a voting strategy, the trading day is

classified as a specific pattern (i.e. buy, sell or no-action) with the largest votes. If no pattern takes only the largest votes, the trading signal is no-action for the next trading day. Fig. 5 provides a simple example illustrating the determination of trading actions in the testing period with a 5-NN classifier. Once the trading signal is determined for a trading day in the testing period, corresponding action is made on the next trading day with the opening price. Thus, the proposed method is called BIC-KNN in this paper. Fig. 6 gives a running example demonstrating how a bicluster can be used as a trading rule in the training period and how to determine the trading action for a trading day based on the matching value (RMS) and the 5-NN classifier in the testing period.

E. Experimental methods

To assess the performance of the BIC-KNN, we conduct experiments to make comparisons with four methods: Genetic programming (GP) [12], Technical charting heuristics (TCH) [8], Buy-and-hold (BAH), and Intelligent hybrid system (IHS) [34]. The GP extends classical genetic algorithm by allowing the processing of non-linear structures. The TCH compares historical stock price and volume to archetypal chart patterns and predicts future price behavior based on the degree of match. The BAH implies to buy at the start of the period and sell at its end. The IHS integrates neural networks, Fuzzy logic, and genetic algorithms techniques into the volume adjusted moving average (VAMA) technical indicator for stock trading.

Four different real-world data sets are used for evaluation of the methods. In particular, three data sets were used by the control methods[8] [12] [34], respectively. Dataset 1 including four Canadian companies stocks was used in [12] (see Table III). Dataset 2 including six major world indices (see Table IV) from 07/02/1997 to 11/13/2012 (downloaded from Yahoo Finance [35]) are used for comparisons between the BAH and BIC-KNN. Dataset 3 is the New York Stock Exchange (NYSE) Composite Index covering the period between 08/06/1980 and 06/08/1999 which was used in [8]. The division of the data into the training and testing periods is the same as [8] in order to make an exact comparison. Dataset 4 is the past S&P 500 index that was used in [34]. The training and testing periods in this study are also the same as [34] and the exact time periods used for the experiments are listed in Table V. All historical data consists of the opening price, the highest price, the lowest price, the closing price and the transaction volume for each trading day. In the BIC-KNN, the training period is used to construct the data matrices, discover biclusters, and generate trading rules. With the discovered trading rules, the trading actions can be performed on the testing period to evaluate the profiting performance.

As mentioned above, the evaluation of the detected biclusters are determined by two parameters (i.e. T_{hc} and T_{sd}) that should be carefully assigned as they have important influence on the final profits. To find appropriate values for the parameters, preliminary experiments are performed. Considering the time complexity, we have implemented 10 independent runs for each dataset and tabulated the profits as well as the standard deviations (SD). For each run, T_{hc} and T_{sd} are tuned by a

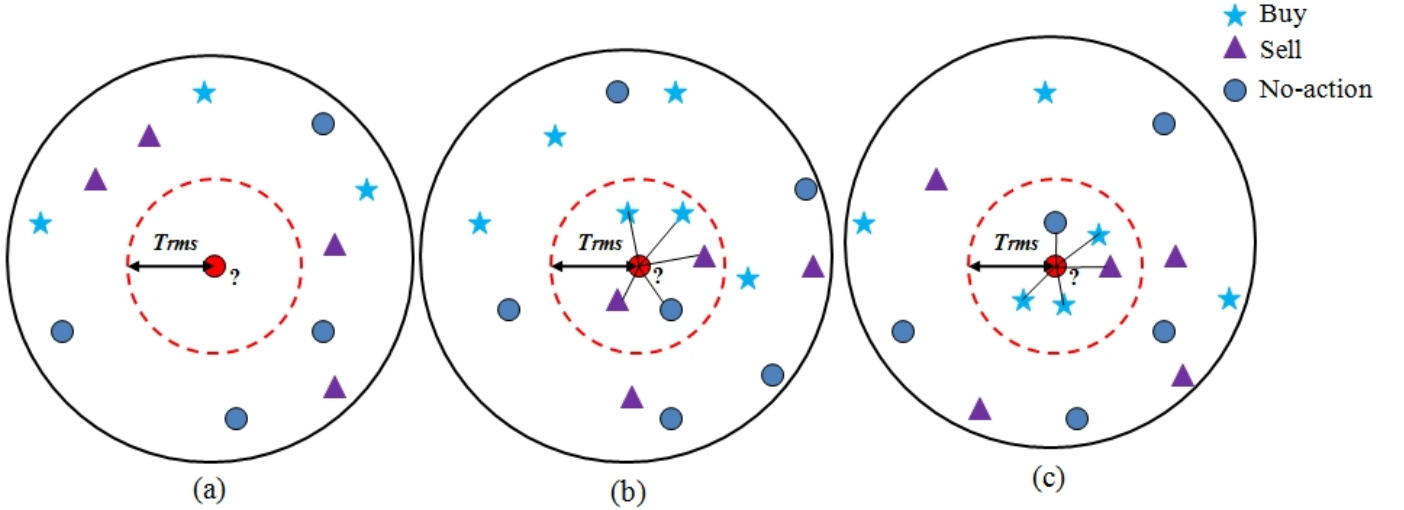


Fig. 5: An illustration on how to use the 5-NN classifier to determine the trading actions in the testing period. (a) There is no trading rule falling into the neighborhood; (b) in the neighborhood, the number of buy signals is the same as that of sell signals, hence the trading action is no-action; and (c) the number of buy signals is the largest, hence the trading action is buy.

TABLE III: DATASET 1: FOUR CANADIAN COMPANIES STOCKS

Activity sector	Company	Symbol	Period
Precious metals	Barrick Gold Corporation	ABX	Training
Pipelines	Trans Canada Pipelines Ltd	TRP	06/30/1992 - 06/25/1999
Oil and gas	Cdn.Occidental Petroleum Ltd	CXY	Testing
Diversified(conglomerate)	Canadian Pacific Ltd	CP	06/28/1999 - 06/30/2000

TABLE IV: DATASET 2: SIX MAJOR WORLD INDICES IN ASIA

Market	Indices	Symbol	Period
Bombay	BSE SENSEX	BSESN	Training
Kuala Lumpur	FTSE Bursa Malaysia KLCI	KLSE	07/02/1997 - 03/03/2008
Korea	KOSPI Composite Index	KS11	Testing
Osaka	NIKKEI 225	N225	03/04/2008 - 11/13/2012
Singapore	STRAITS TIMES INDEX	STI	
Taiwan	TSEC weighted index	TWII	

TABLE V: THE TRAINING AND TESTING PERIODS OF DATASET 4: S&P 500 INDEX

S&P 500 index	Training period	Testing period
Trending-up market	01/01/1998 - 12/30/2002	01/01/2003 - 12/30/2003
Flat market	01/01/1995 - 12/30/1999	01/01/2000 - 12/30/2000
Trending-down market	01/01/1997 - 12/30/2001	01/01/2002 - 12/30/2002

random combination of a range from 0.005 to 0.25 and we therefore can find the best results for each dataset.

IV. EXPERIMENTAL RESULTS

The algorithm is programmed using Matlab (Mathworks, Co., USA). Experimental tests were conducted on a 3.40 GHz PC with an Intel Core i2 Duo CPU. For the training of trading rules, the execution time varies with the sizes of the dataset. The average execution time for dataset 1 (about 2000 days) was approximately 20 seconds, and that for dataset 2 (3830 days) required approximately 40 seconds. For dataset 3 (4748 days), the average execution time is summarized in Table VIII. For dataset 4 (about 1500 days), the computation time in each run was approximately 12 seconds on average.

Tables VI- IX present the average performance for the testing data set of the four datasets using the two trading strategies

in the experiments. The results include the profitability, the SD of profits (for 10 runs) and the number of trades discovered in the testing periods. The BIC-KNN outperforms the other four trading methods in the testing periods, demonstrating significantly promising usefulness.

Specifically, as shown in Table VI the proposed BIC-KNN under the two trading strategies achieves better average profits (39.50% for strategy 1 and 42.35% for strategy 2) than the GP (23.24%). Table VII demonstrates that the average profits made by the BIC-KNN are better than those made by the BAH strategy on all indices. In particular, strategy 1 significantly outperforms the BAH, substantially improving the average profitability by 95.90% over the BAH. In Table VIII, the annual profits from 1982-1999 made by the BAH, TCH and the BIC-KNN, respectively, are listed. Our method has an

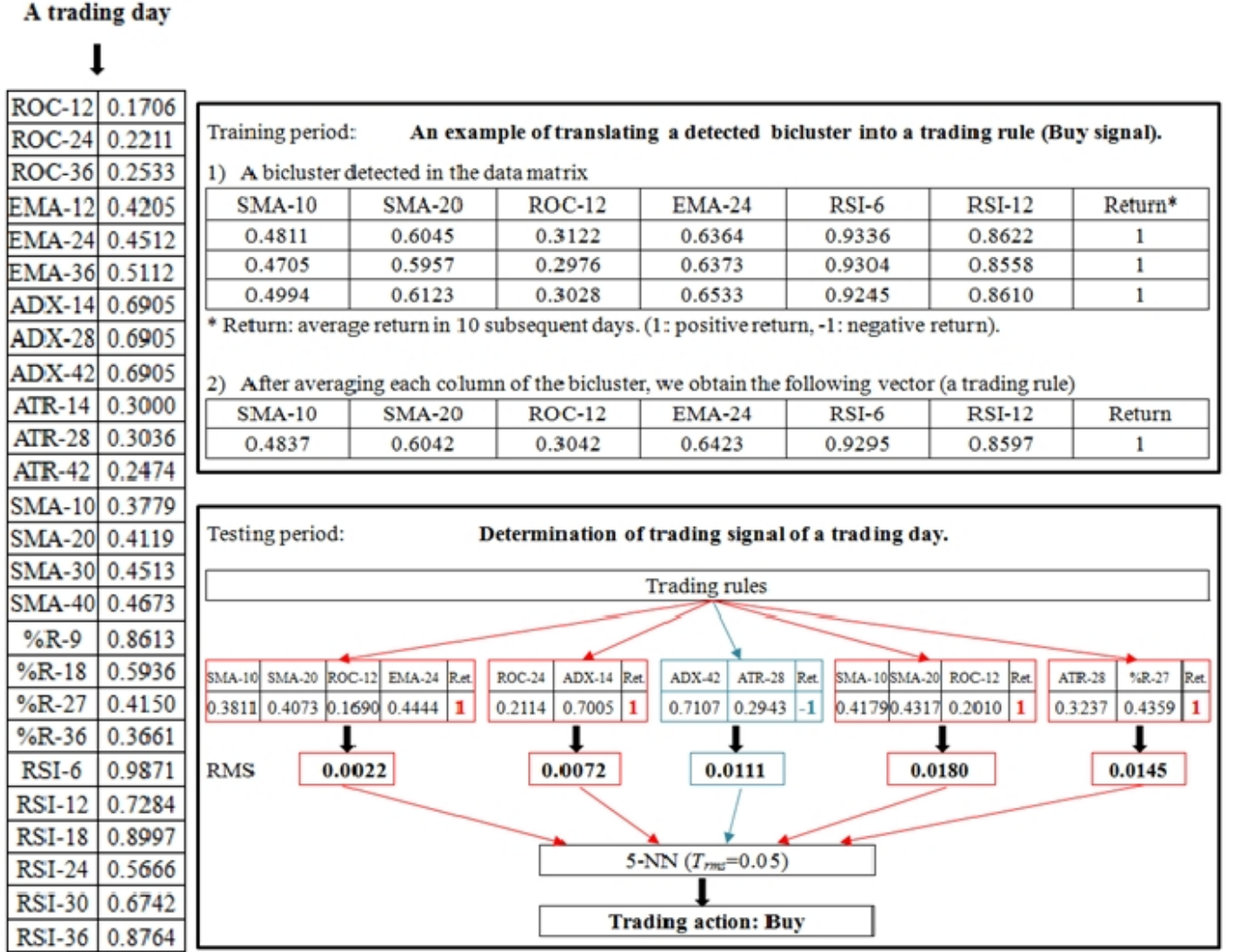


Fig. 6: An example for demonstrating how a detected bicluster is translated into a trading rule in the training period, and how to determine the trading action for a trading day based on the RMS and the 5-NN classifier in the testing period.

improved overall average profit, and outperforms the BAH and TCH in most years. In the testing periods, the TCH method gains 5.5% on average. In contrast, our method averagely gains 17.19% with strategy 1 and 16.30% with strategy 2, respectively. In another word, the BIC-KNN further improves the average profitability by 11.69% with strategy 1 and 10.80% with strategy 2 over the TCH methods, respectively. The average number of trades for the BIC-KNN (i.e. 13.94 trades for strategy 1 and 8.17 trades for strategy 2) is significant decreased comparing to the TCH (236 trades on average). Obviously, lower number of trades help reduce transaction costs in practices.

In Table IX, although it gives slightly poor results in trending-up market, the BIC-KNN significantly outperforms the IHS in trending-down market and obtains similar performance in the flat market. It can be concluded that most of the predictions on the future trends are correct in the BIC-KNN method, hence double positive profits can be achieved. The SDs of trading rules with strategy 1 are higher than those

with strategy 2. Thus, the average fluctuation range of profits for strategy 1 is higher than that of strategy 2. Although some trades yield negative returns using our method (e.g. dataset 1: TRP), the trading rules discovered by the proposed BIC-KNN are capable of making more profits than the other four methods. The results are an encouraging evidence indicating that the BIC-KNN is capable of finding more profitable trading rules in financial markets.

Figs. 7-10 show more understandable examples by marking the buy and sell trading points in the testing periods of four stocks (i.e. ABX, BSESN, S&P 500 index trending-up and trending-down markets). These trading points are derived from the trading rules discovered in the training periods by the BIC-KNN. It is observed that the trading rules can successfully detect correct buy points at the bottoms and correct sell points at the tops.

V. DISCUSSION AND CONCLUSION

In this paper, we propose to use a novel intelligent trading method incorporating a biclustering algorithm and the K-NN

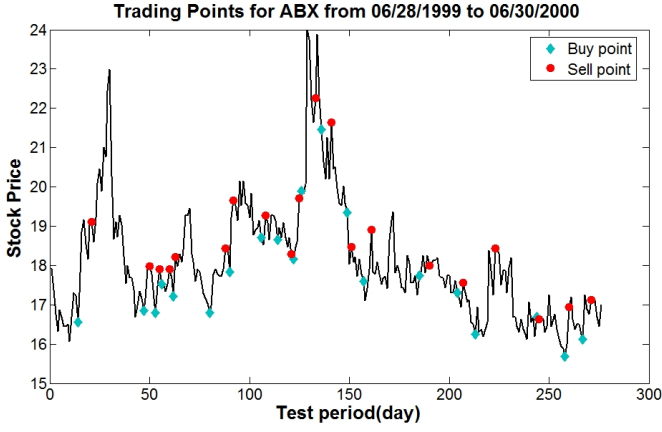


Fig. 7: Trading points for ABX from 06/28/1999 to 06/30/2000.

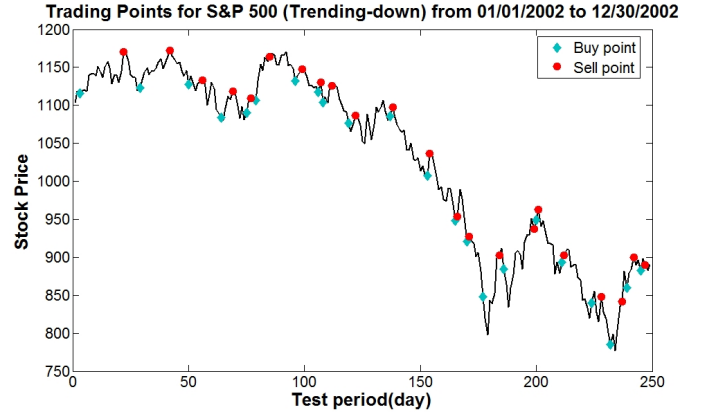


Fig. 10: Trading points for S&P 500 index (Trending-down market) from 01/01/2002 to 12/30/2002.

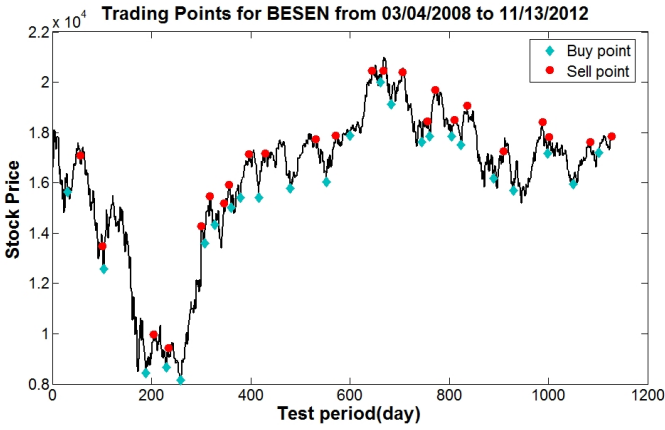


Fig. 8: Trading points for BSESN from 03/04/2008 to 11/13/2012.

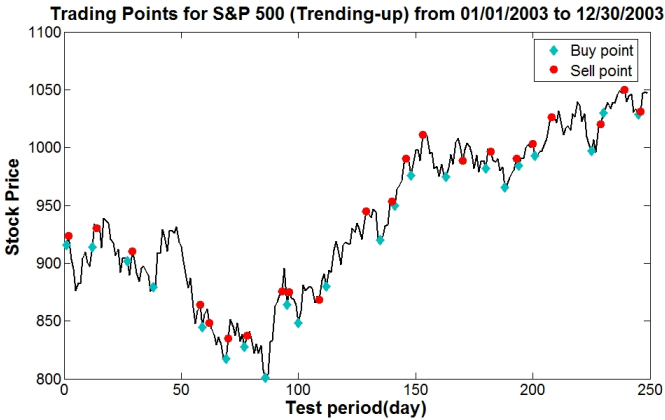


Fig. 9: Trading points for S&P 500 index (Trending-up market) from 01/01/2003 to 12/30/2003.

method to discover trading rules based on a combination of technical indicators in financial markets. To the best of our knowledge, this is the first attempt to apply biclustering algorithm to financial data series for finding trading rules. Seven active technical indicators (ROC, EMA, ADX, ATR, SMA, WMS and RSI) with different time span parameters

and future returns are incorporated to form a data matrix. The biclustering algorithm is designed to discover biclusters with constant columns in the data matrix. The detected biclusters are regarded as trading rules and grouped into buy, sell and no-action signals. A 5-NN classification method is used to determine the trading action of a trading day in the testing period. The proposed algorithm (BIC-KNN) is implemented on four datasets and has been compared the average performance with four existing methods. The results demonstrate that our method significantly outperforms its counterparts. Furthermore, the proposed method is a framework that can be extended to add more technical indicators, different time spans and trading terms, which makes it a general and flexible model for investors in various financial markets.

Nevertheless, there are some limitations when using the proposed method. Firstly, we ignored the missing data in the original data matrix, due to the integrity of the data may affect the efficiency of the data analysis and the results of the experiments, it is necessary to estimate missing values to maintain data integrity. Secondly, we selected only a small number of technical indicators to generate the trading rules. As is well known to investors, there are a large variety of technical indicators for investment. Therefore, it is expected that more robust and effective trading rules could be mined using more indicators to generate even better trading systems. Moreover, more selections of the time span for each indicator may be helpful to discover the optimal indicator combinations, which could provide more robust trading rules. Thirdly, several parameters (i.e. T_{hc} , T_{sd} , T_{pre} and T_{rms}) need to be carefully set when mining the trading rules. T_{rms} is used for determining the distance for the KNN algorithm and is adaptively set by the mean value. Obviously, smaller T_{rms} will guarantee the similarity between the trading days and the discovered trading rules. T_{hc} and T_{sd} are used for mining biclusters in the training period. They are tuned by a random combination of a range from 0.005 to 0.25 and then the best result for each dataset is reported. T_{pre} is the pre-defined threshold used for obtaining more reliable trading signals in the testing period. Larger T_{pre} leads to more reliable trading signals. Nevertheless, three parameters have to be empirically

set with respect to preliminary trials in current study. However, in financial practices, this would be inconvenient for investors. A possible solution is to use learning algorithms to find the optimal settings for these parameters. Fourth, we have only considered the periodic cycle length (i.e. 10 days), which predicts the future trend in short-term. However, investors may plan to trade in the middle-term or long-term. With different trading cycles, the mined trading rules may be quite different. Fourth, the current method for selecting biclusters as trading patterns is relatively simple and may not be adequately reliable.

According to these limitations, future work will extend the research in this study to a more general model, to develop various trading systems with improvements. First, methods of completion of arbitrary matrices from limited information will be introduced to our work, such as the method proposed by Hu et al.[36]. Second, more technical indicators with a larger variety of time spans will be considered for formation of data matrices. Third, intelligent learning algorithms (e.g. multiobjective genetic programming (MOGP) [37] or particle swarm optimization algorithm) will be applied to find the optimal parameters with respect to the metrics of profit ratings. Fourth, different trading cycles will be taken into account to generate more complicated and more profitable trading strategies. Finally, the validations of the detected biclusters will be performed with respect to some measures [38] [39] [40], and the classification of trading signals can be improved by applying some most advanced learning models, such as the domain adaption learning method [41].

In conclusion, this study has innovatively proposed to use a biclustering algorithm and the K-NN classification method to discover trading rules, and apply them to real financial markets. It is the first attempt to use biclustering algorithm on financial data series. Experimental results demonstrate that the proposed method outperforms four existing trading strategies, indicating its sound performance for trading in financial markets. We expect that the novel idea of converting the biclusters into trading rules will lead to a new research topic in finance theory and applications.

ACKNOWLEDGMENTS

This work is supported by the National Basic Research Program of China (973 Program) (Grant No. 2012CB316400), the National Natural Science Foundation of China (Grant Nos: 61125106 and 61372007), the Australian Research Council Linkage Project (No. 140100569), the Projects of Innovative Science and Technology, Department of Education, Guangdong Province (No. 2013KJCX0012), and the Key Research Program of the Chinese Academy of Sciences (Grant No. KGZD-EW-T03).

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TABLE VI: COMPARISON BETWEEN THE GP AND BIC-KNN ON FOUR CANADIAN STOCKS. “PROFITS (%)” IS THE AVERAGE EXCESS RETURN OF 10 RUNS. “TRADES” IS THE AVERAGE NUMBER OF TRADES.

Stock	GP Profits (%)	Strategy 1			BIC-KNN Strategy 2		
		Profits (%)	SD	Trades	Profits (%)	SD	Trades
ABX	31.76	70.59	34.05	45	68.64	15.12	23
CP	17.36	46.32	37.56	11	34.50	10.29	23
CXY	29.23	55.49	26.81	38	32.37	8.97	20
TRP	14.62	−14.05	28.48	47	33.87	9.12	26
Average	23.24	39.50	31.73	35.25	42.35	10.88	23

TABLE VII: COMPARISON BETWEEN THE BAH AND BIC-KNN ON SIX MAJOR WORLD INDICES IN ASIA. “PROFITS (%)” IS THE AVERAGE EXCESS RETURN OF 10 RUNS. “TRADES” IS THE AVERAGE NUMBER OF TRADES.

Index	Buy-and-hold Profits (%)	Strategy 1			BIC-KNN Strategy 2		
		Profits (%)	SD	Trades	Profits (%)	SD	Trades
BSESN	33.70	150.06	62.02	117	28.50	3.34	24
KLSE	46.06	65.78	36.12	167	16.24	2.77	22
KS 11	20.07	126.99	28.49	132	38.06	4.75	22
N225	−32.09	89.45	41.89	179	30.92	11.40	19
STI	5.14	93.11	53.48	40	19.09	6.11	19
TWII	1.59	124.46	45.94	161	20.48	6.20	25
Average	12.41	108.31	44.66	132.67	25.55	5.76	21.83

TABLE VIII: COMPARISON BETWEEN THE TCH AND BIC-KNN ON THE NYSE INDEX. “ALL” STANDS FOR ALL TRADING DAYS OF BUY-AND-HOLD STRATEGY. “RULE1” AND “RULE2” REPRESENT TWO VARIATIONS OF THE BULL FLAG TECHNICAL CHARTING HEURISTIC. “PROFITS (%)” IS THE AVERAGE EXCESS RETURN OF 10 RUNS. “N” IS THE AVERAGE NUMBER OF TRADES.

	TCH						BIC-KNN						Average execution time(s)
	All Profits (%)	N	Rule 1 Profits (%)	N	Rule 2 Profits (%)	N	Strategy 1 Profits (%)	SD	N	Strategy 2 Profits (%)	SD	N	
1982	19.2	108	19.8	5	13.9	36	15.98	11.99	10	9.39	5.70	2	3.24
1983	2.1	251	0	0	13.59	2	30.81	26.10	21	26.71	14.75	15	4.78
1984	5.1	252	0	0	9	2	12.61	13.11	19	3.60	2.59	3	6.98
1985	9.9	250	20.3	10	6.4	42	15.74	9.24	22	14.61	2.17	13	10.53
1986	9	252	0	0	0	0	32.31	14.85	24	31.38	7.52	13	14.50
1987	−2.6	253	0	0	8.9	43	23.55	12.82	9	37.72	6.45	8	18.01
1988	5.4	253	0	0	0	0	12.03	25.86	4	11.37	11.57	2	21.80
1989	4.9	252	0	0	2.4	12	18.20	13.14	8	21.90	6.09	8	25.58
1990	3.1	253	15.9	25	0	0	6.61	11.30	30	8.38	5.25	11	31.31
1991	5.7	252	21.1	9	1.7	13	27.30	13.64	4	20.70	9.55	4	30.88
1992	3	254	2.5	2	−0.1	12	11.88	7.84	13	7.31	2.92	5	33.30
1993	1.9	253	0	0	0	0	6.38	8.68	11	7.36	5.38	8	36.29
1994	1.8	251	0.2	31	0	0	2.30	6.40	15	3.02	2.58	6	39.80
1995	10.6	251	13.5	22	10.2	33	20.20	8.71	11	17.79	7.34	11	39.71
1996	7.6	253	0	0	2.3	17	20.50	6.64	24	17.80	2.96	12	44.56
1997	12.1	252	0	0	16.3	7	34.89	12.36	17	28.90	4.79	10	46.47
1998	4.8	252	11.6	20	−15	1	11.51	12.87	7	18.91	10.08	8	52.67
1999	1.8	106	0	0	0	0	6.69	6.23	2	6.64	3.36	8	42.92
Average	5.5	236	11.5	124	7.8	220	17.19	12.32	13.94	16.30	6.17	8.17	27.96

TABLE IX: COMPARISON BETWEEN THE IHS AND BIC_KNN ON THE S&P 500 INDEX (WITHOUT TRANSACTION COSTS). “G/L (\$)” IS THE AVERAGE GAIN OR LOSS OF THE TRADING. “PROFITS (%)” IS THE AVERAGE EXCESS RETURN OF 10 RUNS. “TRADES” IS THE AVERAGE NUMBER OF TRADES.

S&P 500	IHS						BIC-KNN					
				Strategy 1						Strategy 2		
	G-L(\$)	Profits (%)	Trades	G-L(\$)	Profits (%)	SD	Trades	G-L(\$)	Profits (%)	SD	Trades	
Trending-up	238.67	26.88	6	226.67	25.13	12.22	43	135.97	14.13	6.09	8	
Flat market	107.90	8.34	31.20	133.92	9.93	13.89	3	109.87	8.43	6.55	3	
Trending-down	−55.28	−5.59	4.40	154.13	16.45	12.09	38	186.73	18.48	8.7	3	